

## Problem A. Experiments with Gorum

Input file: `expgorl.in`  
Output file: `expgorl.out`  
Time limit: 1 second  
Memory limit: 64 megabytes

Recently Yerzhan invented a new type of laser that is capable of measuring distance to distant objects. As any invention, laser needs testing and Yerzhan wants to test it on a moving animate creature (don't ask the final purpose of this laser). Since using mouses is too mainstream, Yerzhan went to the Forbidden Forest in search of a right creature.

The story of Yerzhan catching Gorum is quite fascinating, but it would be inappropriate to tell it right now. What is more important is that he found the subject of his experiments. The creature's name is Gorum and, despite Yerzhan's efforts, Gorum, being a pretty dumb creature, only learned to strictly perform 5 types of commands, denoted by Latin symbols for convenience:

- "L" — Gorum takes one step to its left — transition from point  $(x, y)$  to point  $(x - 1, y)$ .
- "R" — Gorum takes one step to its right — transition from point  $(x, y)$  to point  $(x + 1, y)$ .
- "F" — Gorum takes one step forward — transition from point  $(x, y)$  to point  $(x, y + 1)$ .
- "B" — Gorum takes one step backwards — transition from point  $(x, y)$  to point  $(x, y - 1)$ .
- "I" — Gorum takes a shiny ring with glowing texts out of his pocket and doesn't move at all.

For experiment purposes Yerzhan located his laser in point with coordinates  $(Laser_x, Laser_y)$  on a plane in Euclidean space. Yerzhan also taught Gorum to understand and perform a list  $T$  of these 5 commands, where  $T$  is a string containing the commands in the order Gorum must perform them. Gorum starts at point  $(Gorum_x, Gorum_y)$ .

Your task is to output the minimal and maximal distances to Gorum detected by the laser. Your answer will be considered correct if the absolute or relative errors of the two numbers don't exceed  $10^{-9}$ .

### Input

First two lines of input contain a natural number  $K \leq 10^5$  and a string  $S$  ( $|S| \leq 10^4$ ), consisting of symbols "LRFBI". To obtain the list of commands  $T$ , simply concatenate  $S$   $K$ -times to itself (in other words  $T = S^K$ ).

The last two lines contain two pairs of numbers: coordinates of location of the laser  $(Laser_x, Laser_y)$  and of Gorum  $(Gorum_x, Gorum_y)$ .

All coordinates are integer numbers, not exceeding  $10^4$ .

### Output

Two real numbers — minimal and maximal detected distances. Absolute or relative errors of the numbers must not exceed  $10^{-9}$ .

### Examples

<code>expgorl.in</code>	<code>expgorl.out</code>
100000 LRFBI 10000 10000 10000 10000	0.000000000000 1.000000000000

### Note

In 40% of testcases  $|S| \leq 2 \times 10^3$ ,  $K \leq 2 \times 10^4$ .

## Problem B. Riddick's Cube

Input file: `riddicks.in`  
Output file: `riddicks.out`  
Time limit: 2 seconds  
Memory limit: 64 megabytes

It is well known, that the most sold toy in history is Rubik's Cube. In mere 40 years 350 millions items were sold. A famous Kazakhstani businessman decided to repeat that success, by creating a simpler version of this puzzle. Riddick's Cube, the ingenious invention of the businessman, is an  $N \times M$  rectangle consisting of  $1 \times 1$  cells, each of which is colored in some color. The rules of the puzzle are simple: in a single move it is allowed to cyclically move any row or column by one cell in any direction (rows are moved left or right, columns are moved up or down). For example, this is how 2-nd row is moved right and how 3-rd column is moved up::

1 2 3 4		1 2 3 4		1 2 3 4		1 2 7 4
5 6 7 8	=>	8 5 6 7		5 6 7 8	=>	5 6 11 8
9 10 11 12		9 10 11 12		9 10 11 12		9 10 3 12

A configuration of the puzzle is called final, iff either each of the rows contains cells of the same color or each column contains cells of the same color.

The businessman is concerned about the solvability of his puzzle and so he wants to estimate its complexity before starting the sales. And he gives that task to you. To estimate the complexity we will simplify the rules: you can shift some columns(possibly none) and then — some rows(possibly none).

You are given a configuration of one of the Riddick's Cubes. If a final configuration can be reached using the simplified rules, then the complexity of the configuration is equal to the minimal number of moves, leading to a final configuration. If a final configuration cannot be reached using the simplified rules, then the Cube is said to be mega complex and its complexity is equal to 100500 (probably, the puzzle can still be solved using the normal rules, but it's too complex).

### Input

First line of input contains two integer numbers  $N$  and  $M$  ( $1 \leq N, M \leq 5$ ). The following  $N$  lines contain  $M$  integer numbers each — the description of the puzzle. Each number describes a color in which a corresponding cell is colored. The color numbers are integer numbers in range from 1 to 100. It is not guaranteed that the given configuration is solvable using even normal rules.

### Output

Output one integer number — complexity of the given configuration of the puzzle.

### Examples

<code>riddicks.in</code>	<code>riddicks.out</code>
2 3 1 2 1 2 3 3	2
2 3 2 2 1 1 2 1	100500

## Problem C. Schools

Input file:            `school.in`  
Output file:           `school.out`  
Time limit:            2 seconds  
Memory limit:         256 megabytes

Recently Akim of some state decided to open exactly  $M$  music and  $S$  sports schools to support education in the state. There are  $N$  different cities in the state. For each of the cities both the number of students ready to study in music school and the number of students ready to study in sports school is known. Being a big fan of efficiency, Akim doesn't want to open more than one school in any city (it's possible that he won't open any school in some cities).

You, as Akim's consultant, are given a task of developing a plan that would maximize the number of students that would study in the newly opened schools in the state.

### Input

First line of input contains three integer numbers:  $N$  ( $1 \leq N \leq 300000$ ),  $M$ ,  $S$  ( $0 \leq \min(M, S)$ ,  $M + S \leq N$ ) — the number of cities in the state, the number of music and sports schools that Akim wishes to open respectively.

Each of the following  $N$  lines contains two integer numbers:  $A_i$  ( $1 \leq A_i \leq 10^5$ ) and  $B_i$  ( $1 \leq B_i \leq 10^5$ ) — the number of students in the  $i$ -th city that wish to study in music and sports school respectively.

### Output

Output one integer number — the number of students that will study in the newly opened schools in an optimal plan.

### Examples

<code>school.in</code>	<code>school.out</code>
3 1 1 5 2 4 1 6 4	9
7 2 3 9 8 10 6 3 5 1 7 5 7 6 3 5 4	38

## Problem D. Special graph

Input file: `specialg.in`  
Output file: `specialg.out`  
Time limit: 1 second  
Memory limit: 64 megabytes

You are given a directed graph with  $N$  vertices. The special thing about the graph is that each vertex has at most *one* outgoing edge. Your task is to answer the following two types of queries:

- 1  $a$  — delete the only edge outgoing from vertex  $a$ . It is guaranteed that the edge exists.  $1 \leq a \leq N$
- 2  $a b$  — output the length of the shortest path from vertex  $a$  to vertex  $b$ , if the path exists. Otherwise output “-1” without quotes.  $1 \leq a, b \leq N$

### Input

First line of input contains a natural number  $N \leq 10^5$  — the number of vertices in the graph.

The following line contains  $N$  integer numbers,  $i$ -th number is  $next_i$  ( $0 \leq next_i \leq N$ ), meaning that there is an edge from vertex  $i$  to vertex  $next_i$ . If  $next_i = 0$ , assume that there is no outgoing edge from vertex  $i$ .

Third line contains a natural number  $M \leq 10^5$  — the number of queries.

The following  $M$  contain a query each. Queries are given in the manner described above.

### Output

On the  $i$ -th line output the answer for the  $i$ -th query of type 2  $a b$ .

### Examples

<code>specialg.in</code>	<code>specialg.out</code>
6	4
3 3 4 5 6 4	2
6	-1
2 1 6	-1
2 1 4	-1
2 1 2	
1 3	
2 1 6	
2 1 4	
4	1
4 4 1 3	3
5	1
2 2 4	
2 2 1	
1 4	
1 2	
2 3 1	

### Note

In 50% testcases  $N \leq 2 \times 10^3, M \leq 2 \times 10^4$ .

## Problem E. Crazy old lady

Input file:            crazy.in  
Output file:           crazy.out  
Time limit:            2 seconds  
Memory limit:         64 megabytes

The following problem is a variation of a well known puzzle in the Probability theory. There are  $N$  seats on a plane and all of the seats are assigned to passengers. Passengers are asked to enter the plane, one at a time, in order of their seats, from 1 to  $N$  (the passenger that is assigned seat number 1 enters first, next enters the passenger that is assigned seat number 2, and so on...).

As you might have guessed, queues are too mainstream for a crazy old lady, so she usually goes ahead of everyone and enters first (despite the fact that she might not be assigned the first seat), furthermore she takes some seat that she likes (by chance, it may happen to be her own seat).

After she has taken a seat, the next passengers enter with respect to their seat number (as described above) and take seat as follows:

- if his/her seat is vacant, then he/she takes this seat.
- but if his/her seat is already taken, he/she takes any of the remaining seats.

Which seat takes the last passenger? The answer is simple: the last passenger takes either his own seat or the seat of the crazy old lady!

Assume that crazy old lady occupy seat  $j$ , which is not her own. When passenger that was assigned the seat  $j$  will enter, he/she will have to take some other seat from a set of free seats. This situation then may repeat with next passengers. But when some passenger take the seat of old crazy lady, obviously (!) all of the following passengers take their own seats. In this problem we would like to know the original seat of old crazy lady.

### Input

Input file may contain several tests. First line of Input contains integer  $T$  — the number of tests ( $1 \leq T \leq 10$ ). Each of the next  $T$  lines contains  $N + 1$  numbers, separated by space, first is  $N$  ( $1 \leq N \leq 10^3$ ), then  $N$  numbers follow: the seats taken by passengers in order of their entrance ( $p_1, p_2, \dots, p_N$  - where  $p_i$  means that the passenger that was  $i$ -th to enter took seat  $p_i$ ). Input is guaranteed to be correct, i.e. to satisfy conditions of the problem statement.

### Output

Output the seat of old crazy lady, if it can be determined uniquely, otherwise, output 0.

### Examples

crazy.in	crazy.out
2	0
2 2 1	1
4 2 3 1 4	

### Note

In test case 2 2 1 we cannot uniquely determine answer, as soon as passenger 1 is old crazy lady that take different seat, and passenger 2 may be also old crazy lady that take her own seat.

## Problem F. Luxury burrow

Input file:            **burrow.in**  
Output file:           **burrow.out**  
Time limit:            2 seconds  
Memory limit:         64 megabytes

Hobbit Bilbo is very tired from his adventures and decided to build a new burrow. The hill, where he plans to buy some land, has a shape of a rectangle and it can be represented as a table consisting of  $N$  rows and  $M$  columns (rows and columns are numbered starting from 1, where 1 corresponds to the topmost row and the leftmost column). Each cell of the table corresponds to a  $1 \times 1$  square piece. Hobbits like simple shapes, that's why Bilbo intends to buy a plot of land of a rectangular shape, with sides parallel to the sides of the hill. In other words he chooses  $x_1, x_2, y_1, y_2$  ( $x_1 \leq x_2, y_1 \leq y_2$ ) and buys all cells  $(x, y)$ , such that  $(x_1 \leq x \leq x_2)$  and  $(y_1 \leq y \leq y_2)$ .

After all adventures he took part in, Bilbo is very rich and is not worried about the total price. However, he thinks a lot about his reputation and thus the price of the cheapest cell he will buy must be as high as possible. He also wants his new burrow to be enough to fit all of his furniture, that means the square of a rectangular plot he will buy has to have an area greater than or equal to  $K$ . If there are multiple possible plots, Bilbo chooses the one with the largest area.

Bilbo asks you to find the best plot of land for him.

### Input

The first line of input file contains three numbers  $N, M$  and  $K$ , divided by exactly one space — the number of rows, the number of columns and the minimal possible square of land plot Bilbo can live on, respectively. Each of the following  $N$  lines contains  $M$  numbers — the prices of the corresponding cells. Hence, the number  $j$  in the line  $i + 1$ , corresponds to the cell  $(i, j)$ .  $N$  and  $M$  are positive integers and do not exceed 1000,  $K$  is positive integer and does not exceed the total number of cells in the table, all prices belong to range from 1 to  $10^9$ , inclusive.

### Output

As the answer, output two numbers separated by space. First goes the price of the cheapest cell in the resulting rectangular plot. Second is the total square of this plot.

### Examples

burrow.in	burrow.out
3 3 3 1 1 1 1 2 2 1 2 2	2 4
1 10 5 4 3 2 5 10 7 6 5 1 100	5 5
3 5 2 5 7 5 5 5 8 5 5 7 5 8 5 8 8 8	8 3

### Note

In 40% testcases  $M, N \leq 200$ .

In 64% testcases  $M, N \leq 400$ .

## Problem G. Round words

Input file: `rowords.in`  
Output file: `rowords.out`  
Time limit: 2 seconds  
Memory limit: 128 megabytes

After the recent apocalypse, Azamat, finally, learned about the largest common subsequences of two strings and now he is interested, what will be the largest common subsequence of two round words?

In a round word there is no difference from which symbol the word starts and in which direction it is read.

For instance, the round word “algorithm” can be read as “rithmalgo” and as “oglamhtir”.

For usual words “algorithm” and “grammar” the longest common subsequence length is 3 (the word “grm”), and for round variant of the same word the length of the longest common subsequence is 4 (the word “grma”).

Azamat quickly found out that the standard algorithm cannot get right answer for round words. Write the program which will do that for him.

### Input

Two lines contain one word each. Words are non-empty and the length of each words doesn't exceed 2000 characters.

### Output

The single line must contain one integer number — the length of the longest common subsequence of the given round words.

### Examples

<code>rowords.in</code>	<code>rowords.out</code>
<code>algorithm</code> <code>grammar</code>	4

## Problem H. Trading

Input file:            **trading.in**  
Output file:           **trading.out**  
Time limit:            2 seconds  
Memory limit:         64 megabytes

There are  $N$  small villages close to the highway between Almaty and Taraz numbered from 1 to  $N$ . At the beginning of the winter  $M$  unknown traders began trading knitted hats in these villages. They have only two rules: never trade in one place more than once (one day) and increase the price on hats each day. More formally, each  $i$ -th trader:

1. begins trading in village  $L_i$  with starting price  $X_i$ .
2. each day he moves to the next adjacent village, i.e. if he was trading in village  $j$  yesterday, then today he is trading in village  $j + 1$ .
3. each day he increases the price by 1, so if yesterday's price was  $x$ , then today's price is  $x + 1$ .
4. stops trading at village  $R_i$  (after he traded his knitted hats in village  $R_i$ ).

The problem is for each village to determine the maximal price that was there during the whole trading history.

### Input

Each line contains two integer number  $N$  ( $1 \leq N \leq 300000$ ) and  $M$  ( $1 \leq M \leq 300000$ ) — number of villages and traders accordingly.

Next  $M$  lines contains 3 numbers each:  $L_i, R_i$  ( $1 \leq L_i \leq R_i \leq N$ ) and  $X_i$  ( $1 \leq X_i \leq 10^9$ ) — numbers of first and last village and starting price for  $i$ -th trader.

### Output

Output  $N$  integer numbers separating them with spaces —  $i$ -th number being the maximal price for the trading history of  $i$ -th village. If there was no trading in some village, output 0 for it.

### Examples

trading.in	trading.out
5 2 1 3 2 2 4 6	2 6 7 8 0
6 4 4 4 3 1 2 5 5 6 1 6 6 1	5 6 0 3 1 2